

# Light Mixture Estimation for Spatially Varying White Balance

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**WB**

A





WB

A





**WB**

A







WB

A





**WB**

**A**





0.02



0.98

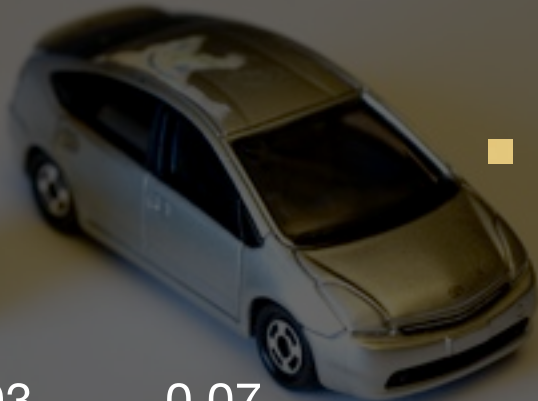
WB

A





0.93



0.07

WB

A





0.37



0.63

WB

A





WB

A





WB

A



Background





Film photographers use color filters during exposure or printing.



Digital cameras simplify this process, but they don't handle mixed lighting.



For mixed lighting, filter each source to emulate single illuminant case.



Barnard [1997]  
... smooth lighting



Ebner [2004]  
... locally neutral



Kawakami [2005]  
... hard shadows



Lischinski [2006]  
... user scribbles

# Overview



The input is a scene illuminated by two light types given by the user.

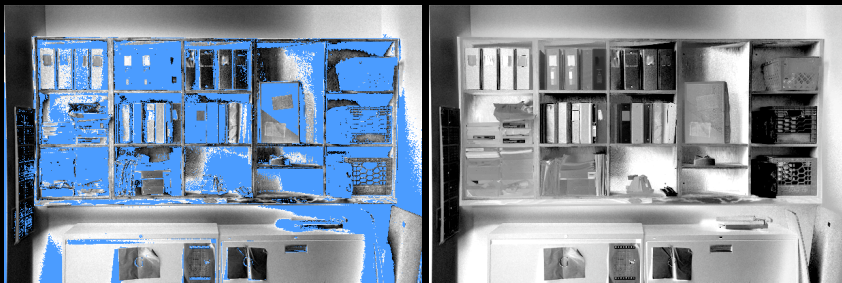


We assume that a few material colors dominate [Omer and Werman 2004].





We vote on these dominant material colors and label pixels accordingly.



We then estimate the light mixture and interpolate missing values.



We use the light mixture to achieve spatially varying white balance.

White Balance

$$\begin{bmatrix} I_R \\ I_G \\ I_B \end{bmatrix} = \begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} k & \begin{bmatrix} L_R \\ L_G \\ L_B \end{bmatrix} \end{bmatrix}$$

Observed pixel color is material color multiplied by scaled light color.

$$\begin{array}{c} W_R \\ W_G \\ W_B \end{array} \cdot \begin{array}{c} I_R \\ I_G \\ I_B \end{array} = \begin{array}{c} R_R \\ R_G \\ R_B \end{array} \cdot \boxed{\begin{array}{c} k \\ \begin{array}{c} L_R \\ L_G \\ L_B \end{array} \end{array}} \div \begin{array}{c} L_R \\ L_G \\ L_B \end{array}$$

Proper white balance is achieved by inverting the light source color.

$$\begin{bmatrix} W_R \\ W_G \\ W_B \end{bmatrix} \cdot \begin{bmatrix} I_R \\ I_G \\ I_B \end{bmatrix} = \begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} & \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \\ \begin{bmatrix} k \end{bmatrix} & \end{bmatrix}$$

Proper white balance is achieved by inverting the light source color.

$$\begin{bmatrix} I_R \\ I_G \\ I_B \end{bmatrix} = \begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \left( k_1 \begin{bmatrix} L_{1R} \\ L_{1G} \\ L_{1B} \end{bmatrix} + k_2 \begin{bmatrix} L_{2R} \\ L_{2G} \\ L_{2B} \end{bmatrix} \right)$$

Our technique assumes two lights.



$$\begin{bmatrix} I_R \\ I_G \\ I_B \end{bmatrix} = \begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \left( \begin{bmatrix} k_1 \end{bmatrix} + \begin{bmatrix} k_2 \end{bmatrix} \right)$$

The goal of white balance is to show the scene under neutral illumination.

$W_R$   
 $W_G$   
 $W_B$

$$\alpha = k_1 \div (k_1 + k_2)$$

Proper white balance is defined by the relative mixture of the lights.

$$\begin{array}{c} I_R \\ I_G \\ I_B \end{array} = \begin{array}{c} R_R \\ R_G \\ R_B \end{array} \cdot \left( k_1 \begin{array}{c} L_{1R} \\ L_{1G} \\ L_{1B} \end{array} + k_2 \begin{array}{c} L_{2R} \\ L_{2G} \\ L_{2B} \end{array} \right)$$

$$\alpha = k_1 \div (k_1 + k_2)$$

Solving for  $\alpha$  is underconstrained since the material color is not given.

[illegible]

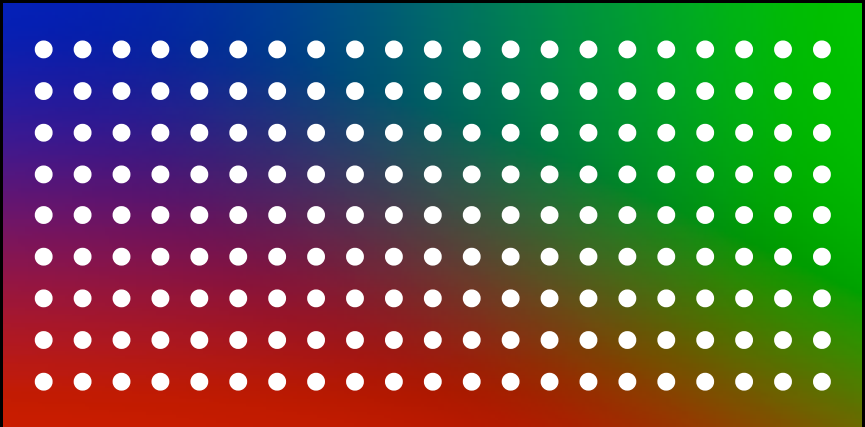
# Material Color Estimation











Sample material colors and find the one that accounts for the most pixels.



Given a candidate material color ...


$$\mathbf{I} = \mathbf{R} \bullet (k_1 \mathbf{L}_1 + k_2 \mathbf{L}_2)$$

... how it could appear in the image?


$$\min \quad \| \mathbf{I} - \mathbf{R} \bullet (k_1 \mathbf{L}_1 + k_2 \mathbf{L}_2) \|$$

... what could be that material color?


$$t \geq \min \| \mathbf{I} - \mathbf{R} \bullet (k_1 \mathbf{L}_1 + k_2 \mathbf{L}_2) \|$$

If this expression holds, we say that the pixel votes for the material color.





48%



**48%**

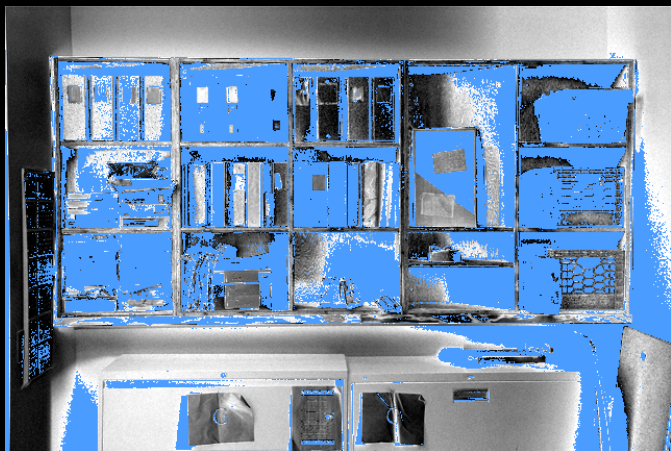
**16%**





48%

16%



# Mixture Interpolation

$$\begin{bmatrix} I_R \\ I_G \\ I_B \end{bmatrix} = \begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \left( k_1 \begin{bmatrix} L_{1R} \\ L_{1G} \\ L_{1B} \end{bmatrix} + k_2 \begin{bmatrix} L_{2R} \\ L_{2G} \\ L_{2B} \end{bmatrix} \right)$$

... assume that  $L_{1B}$  and  $L_{2B}$  are 1.  
 ... divide out the blue channels.

$$\begin{bmatrix} I_{R \div B} \\ I_{G \div B} \end{bmatrix} = \begin{bmatrix} R_{R \div B} \\ R_{G \div B} \end{bmatrix} \cdot \left( \alpha \begin{bmatrix} L_{1R \div B} \\ L_{1G \div B} \end{bmatrix} + (1-\alpha) \begin{bmatrix} L_{2R \div B} \\ L_{2G \div B} \end{bmatrix} \right)$$

$$T \begin{bmatrix} I_{R \div B} \\ I_{G \div B} \end{bmatrix} = \begin{bmatrix} R_{R \div B} \\ R_{G \div B} \end{bmatrix} \cdot \left( \alpha \begin{bmatrix} L_{1R \div B} \\ L_{1G \div B} \end{bmatrix} + (1-\alpha) \begin{bmatrix} L_{2R \div B} \\ L_{2G \div B} \end{bmatrix} \right)$$

That looks exactly like image matting!

$$\begin{bmatrix} I_{R \div B} \\ I_{G \div B} \end{bmatrix} = \begin{bmatrix} R_{R \div B} \\ R_{G \div B} \end{bmatrix} \cdot \left( \alpha \begin{bmatrix} L1_{R \div B} \\ L1_{G \div B} \end{bmatrix} + (1-\alpha) \begin{bmatrix} L2_{R \div B} \\ L2_{G \div B} \end{bmatrix} \right)$$

We perform interpolation using the matting Laplacian [Levin et al. 2006].

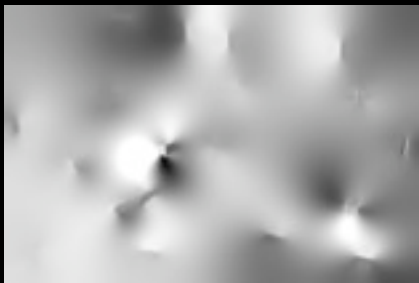


This scene was shot using multiple exposures, so we have ground truth.



We constrain the points in the red squares and interpolate the rest.





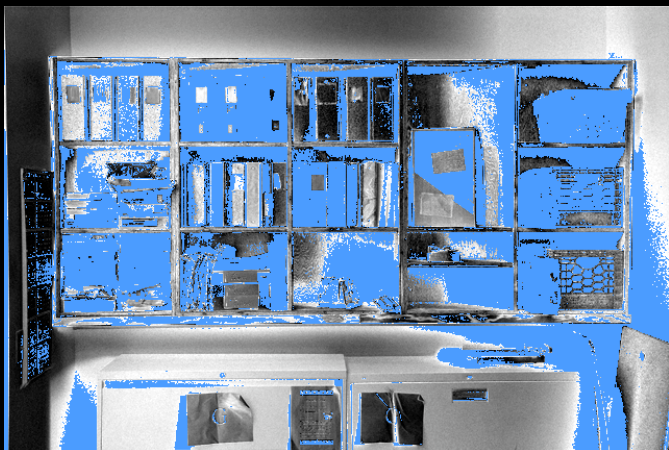
Smooth interpolation is pretty bad.



Edge-aware interpolation is also bad.



Matting Laplacian is much better.







# Results

The following results use synthetic inputs from multiple exposures to allow ground truth evaluations.





Input



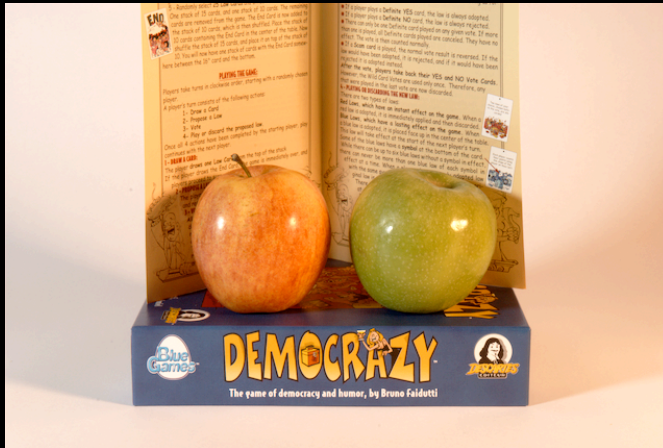
Output



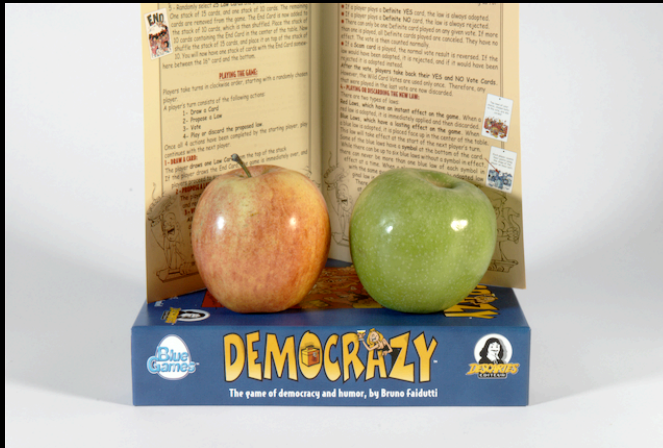
Ground Truth



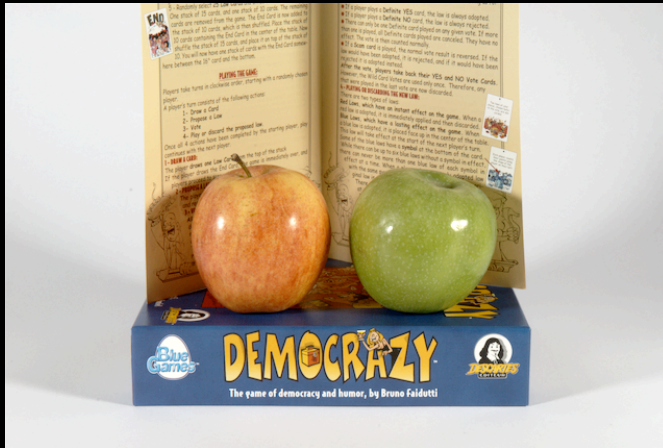
Output



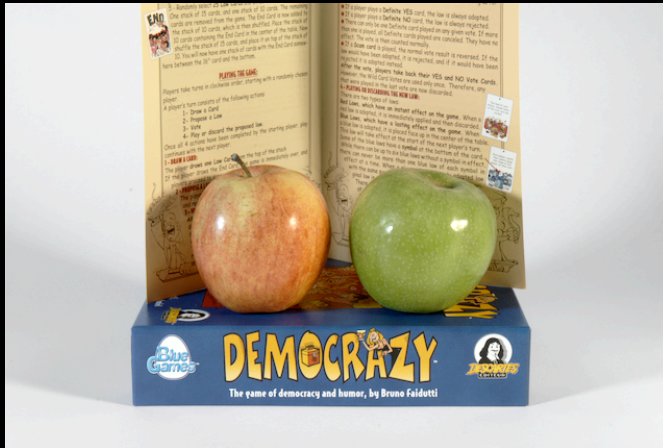
Input



Output



Ground Truth



Output



The following results are from single exposures with real mixed lighting.



Input



Output



Input



Output



Input



Output



Input





Output



Input



Output



Input



Output

Relighting

$$\begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \left( \begin{bmatrix} k_1 & 1 & 1 \end{bmatrix} + \begin{bmatrix} k_2 & 1 & 1 \end{bmatrix} \right)$$

From the white balanced image,  
separate the lighting contributions.

$$\begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \left( \begin{bmatrix} k_1 & 1 & 1 \end{bmatrix} + \begin{bmatrix} k_2 & 1 & 1 \end{bmatrix} \right) \cdot \alpha \div \begin{bmatrix} k_1 & + & k_2 \end{bmatrix}$$

Multiply the white balanced image by  $\alpha$  for the first contribution.



$$\begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} & \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \\ \begin{bmatrix} k_1 \end{bmatrix} & \end{bmatrix}$$

Multiply the white balanced image by  $\alpha$  for the first contribution.

$$\begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} & & 1 \\ k_1 & & 1 \\ & & 1 \end{bmatrix}$$

$$\begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} & & 1 \\ k_2 & & 1 \\ & & 1 \end{bmatrix}$$

Multiply the white balanced image by  $1-\alpha$  for the second contribution.

$$\begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} & 1 \\ k_1 & 1 \\ & 1 \end{bmatrix} \cdot \begin{bmatrix} L_{1R} \\ L_{1G} \\ L_{1B} \end{bmatrix} + \begin{bmatrix} R_R \\ R_G \\ R_B \end{bmatrix} \cdot \begin{bmatrix} & 1 \\ k_2 & 1 \\ & 1 \end{bmatrix} \cdot \begin{bmatrix} L_{2R} \\ L_{2G} \\ L_{2B} \end{bmatrix}$$

We can choose new lights and add the images to get the desired effect.



Input



Output



Output



Input

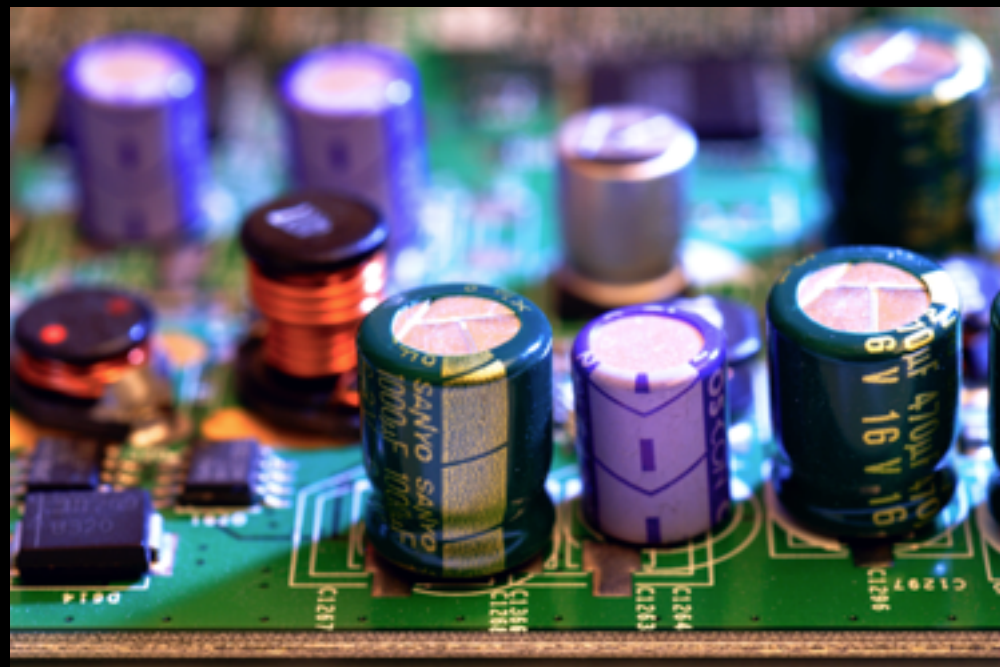


Output

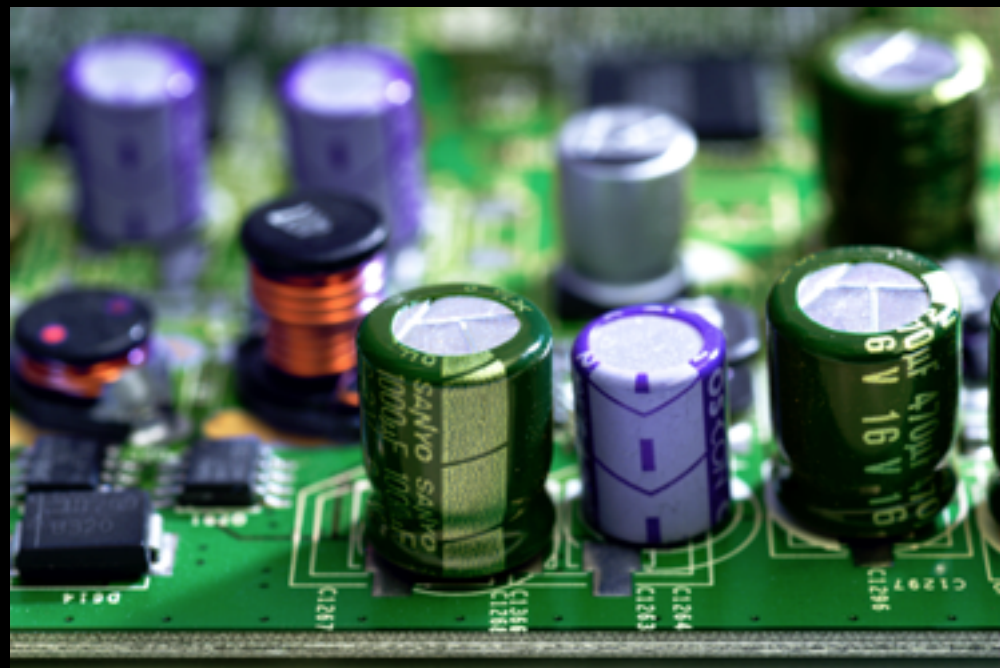




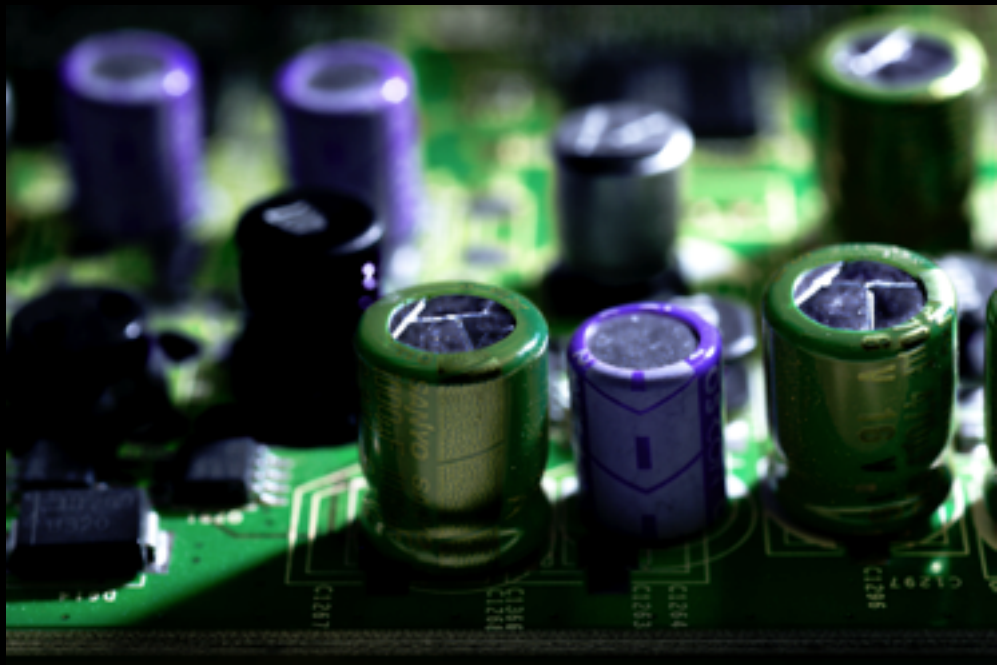
Output



Input



Output



Output

# Discussion

There are two types of light in the scene which the user must identify ...

... can we automate identification?

... why not allow more light types?

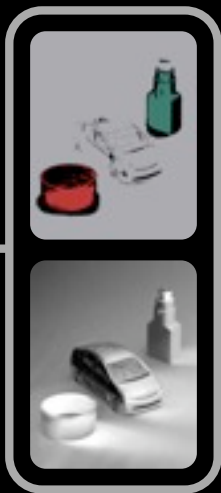
The scene is dominated by a  
small set of material colors ...

The scene is dominated by a  
small set of material colors ...

... which must appear under  
different mixtures of light.









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